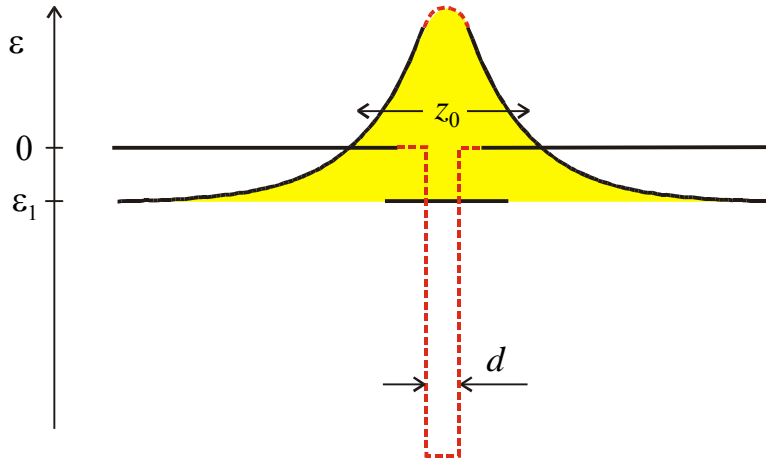


Ultrathin QW's

- Effective mass approximation

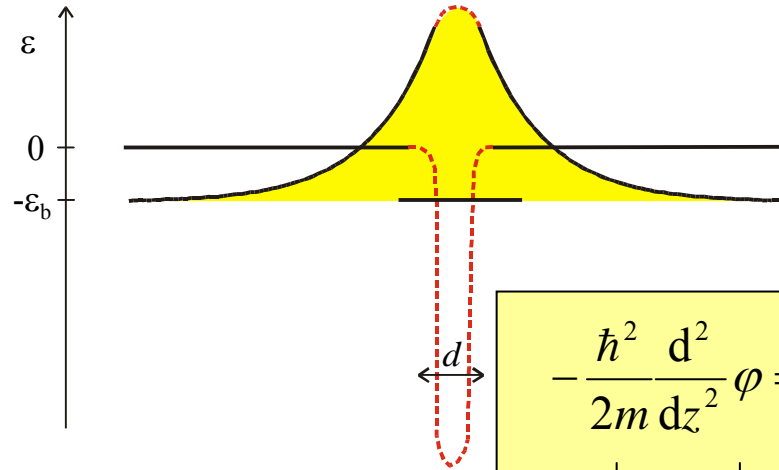


$$\varepsilon_1 = -\frac{\pi^2}{4} \delta^2 U$$

$$\varphi_1 = \sqrt{\alpha_1} \begin{cases} e^{\alpha_1 z}, & z < 0 \\ e^{-\alpha_1 z}, & z > 0 \end{cases}$$

$$\frac{z_0}{d} \sim \frac{1}{\delta^2} \gg 1$$

- Zero-radius potential



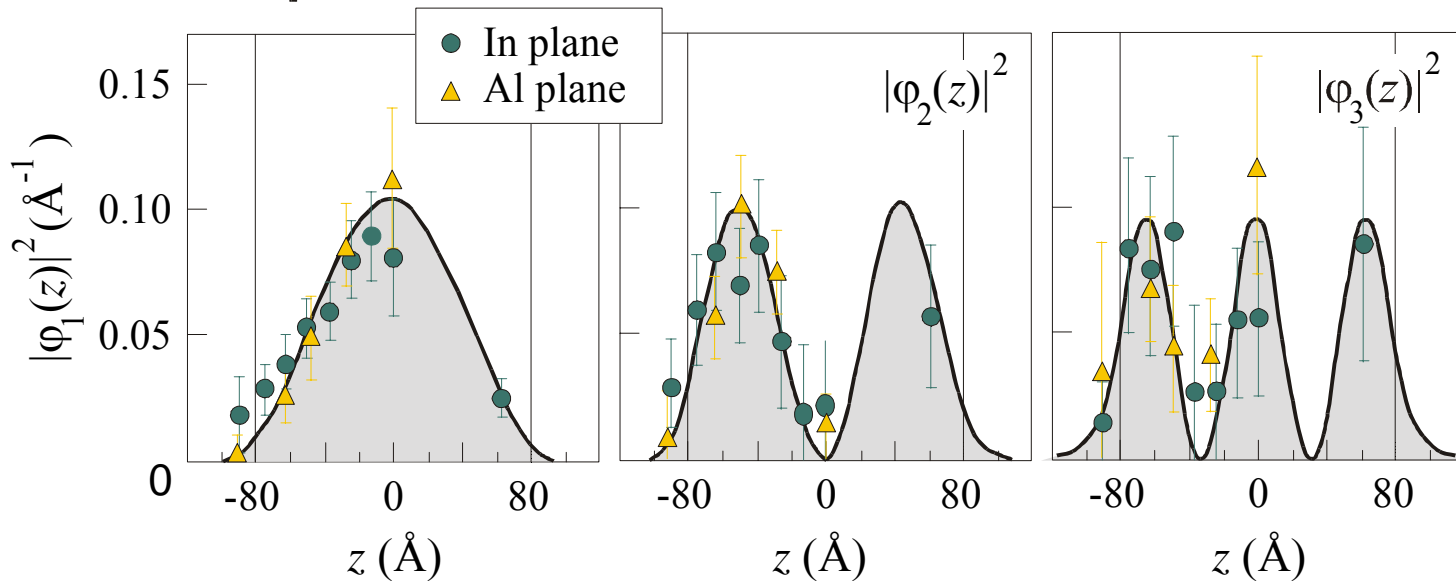
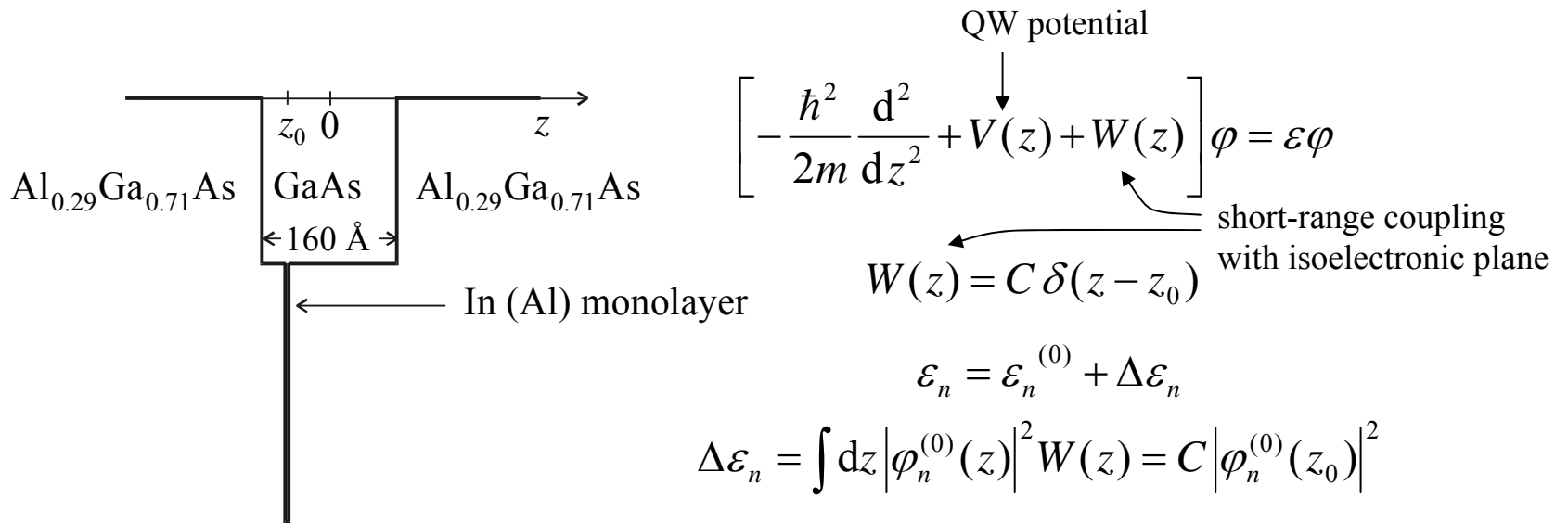
$$\varepsilon_b = \frac{\hbar^2 \alpha^2}{2m}$$

$$\begin{aligned} -\frac{\hbar^2}{2m} \frac{d^2}{dz^2} \varphi &= \varepsilon \varphi \\ \varphi|_{-0} &= \varphi|_{+0} \\ \frac{\varphi'}{\varphi} \Big|_{+0} - \frac{\varphi'}{\varphi} \Big|_{-0} &= -2\alpha \end{aligned}$$

- The Dirac well

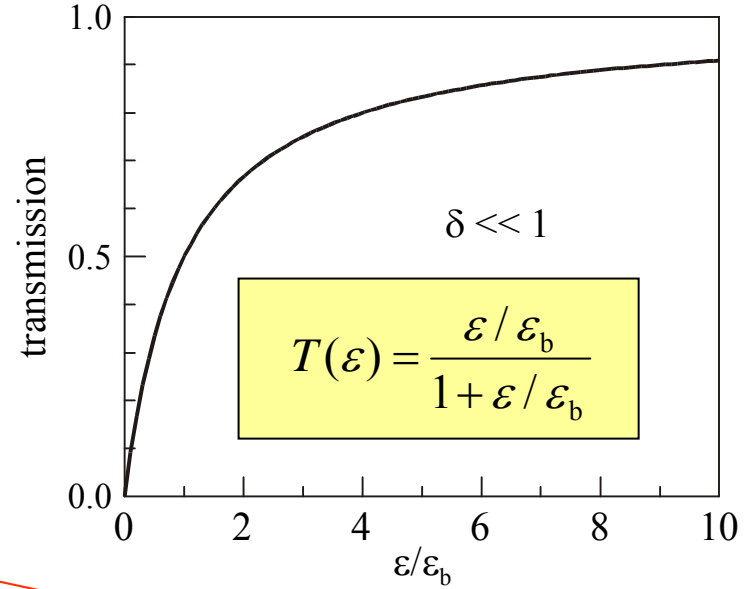
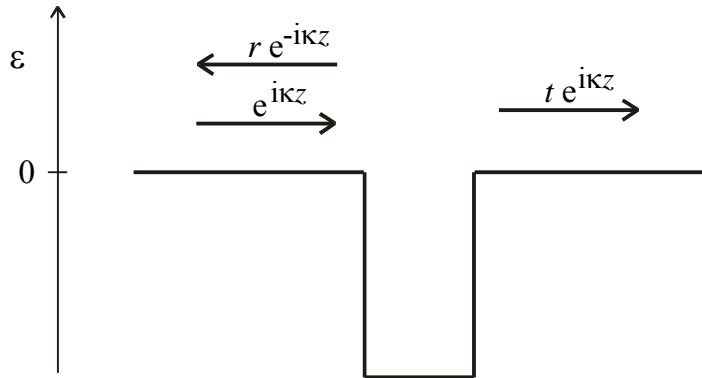
$$\left[-\frac{\hbar^2}{2m} \frac{d^2}{dz^2} - \frac{\hbar^2}{m} \alpha \delta(z) \right] \varphi = \varepsilon \varphi$$

parameter

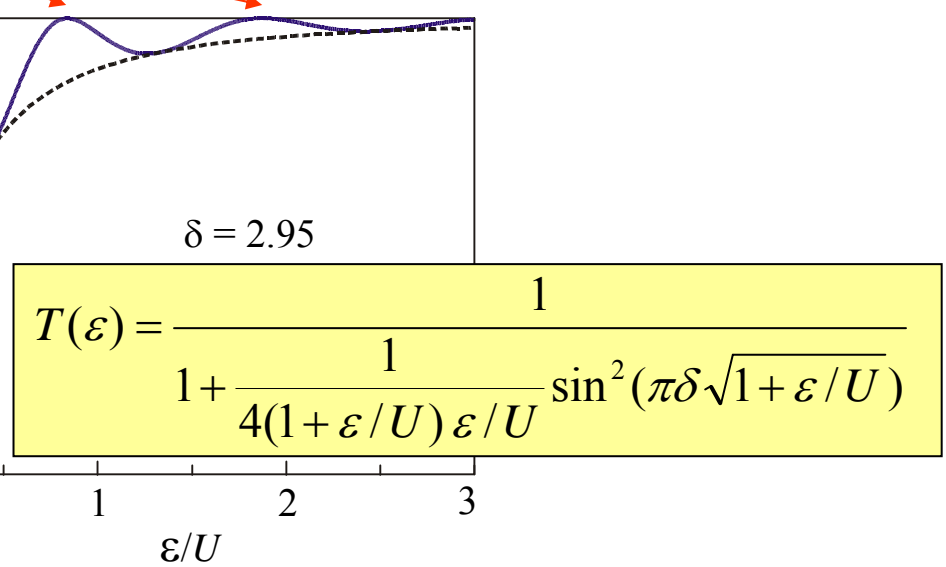
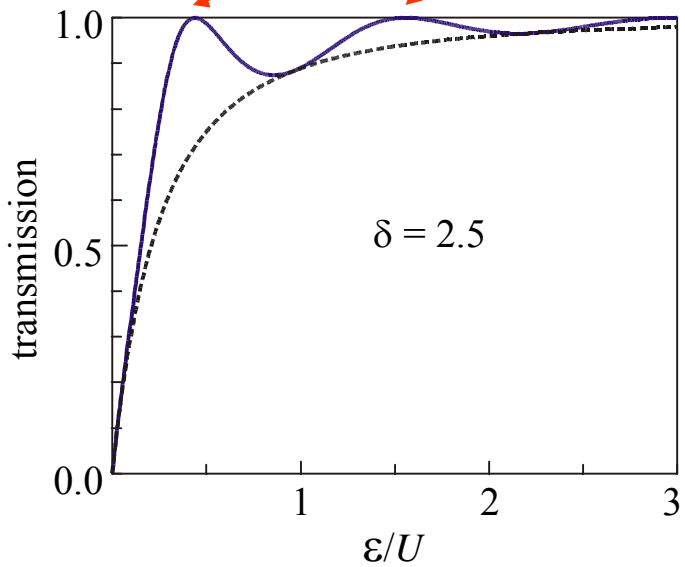


[J.-Y. Marzin and J.-M. Gérard, *Phys. Rev. Lett.*, **62**, 2172 (1989)]

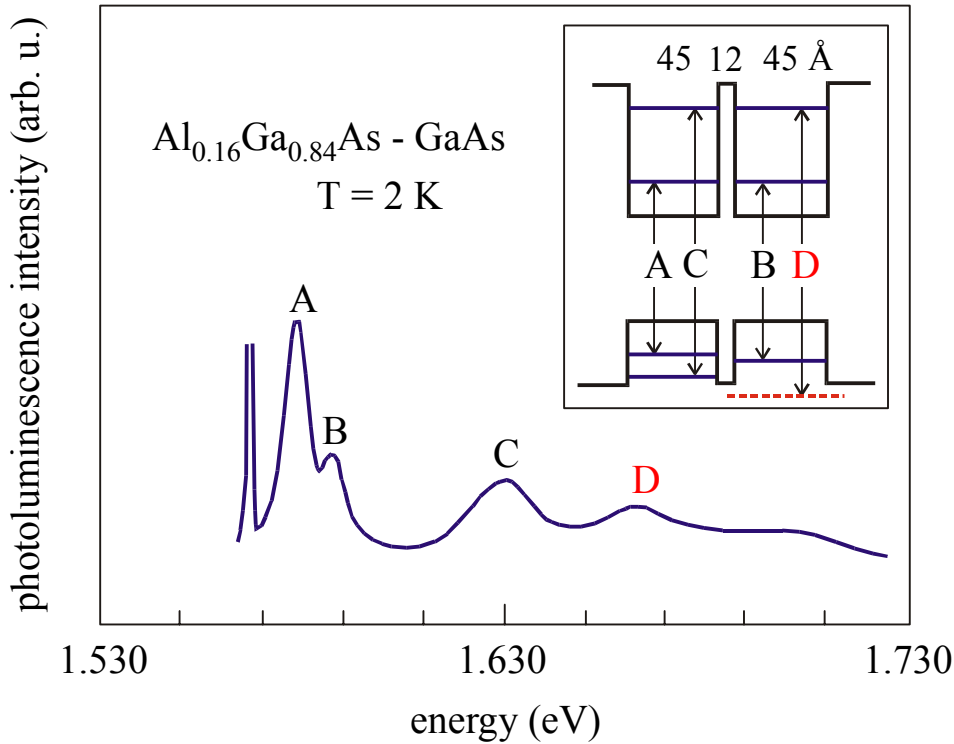
Electrons above QW



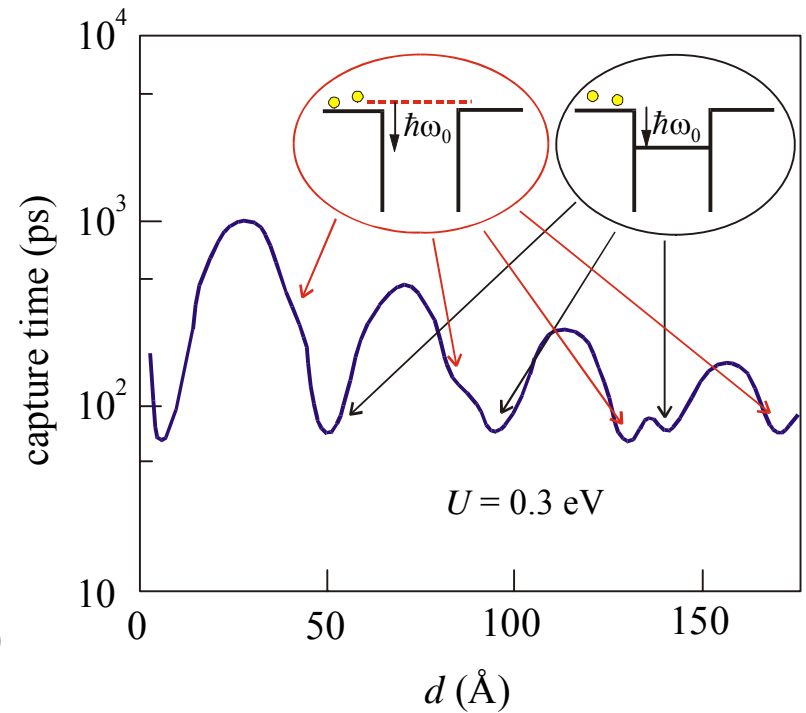
virtual levels
 $\varepsilon + U = Wn^2$



Electrons above QW: Virtual levels

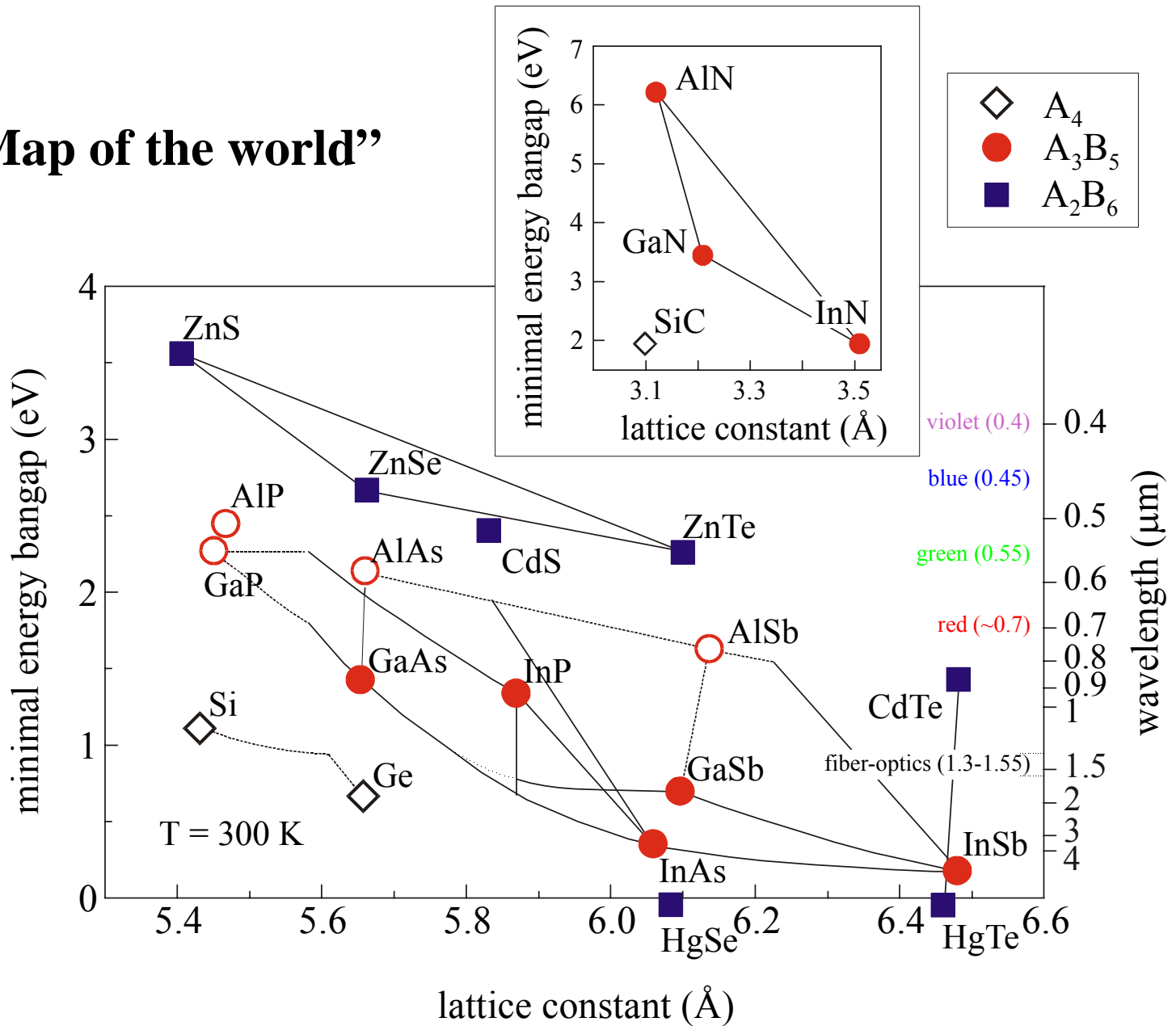


[G. Bastard *et al.*, *Solid State Commun.*, **49**, 671 (1984)]



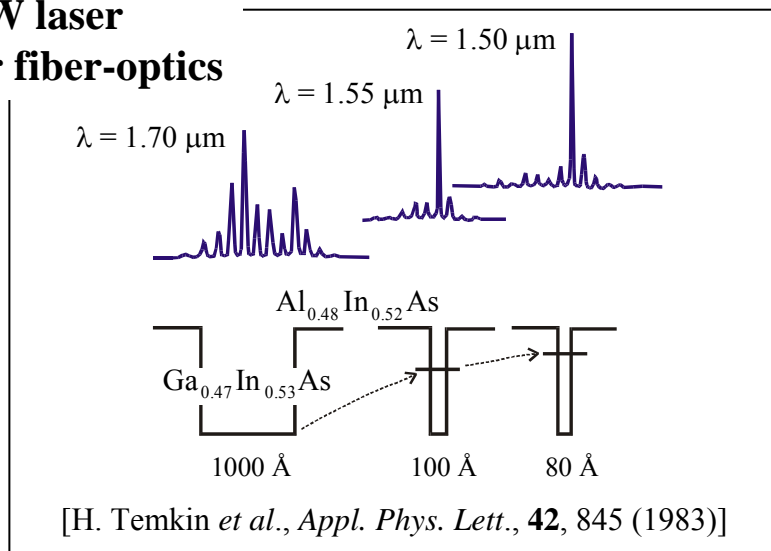
[J. A. Brum and G. Bastard, *Phys. Rev. B*, **33**, 1420 (1986)]

“Map of the world”

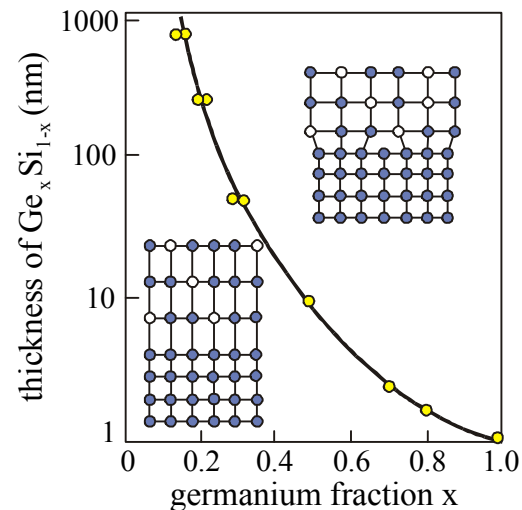


Band structure engineering

**QW laser
for fiber-optics**

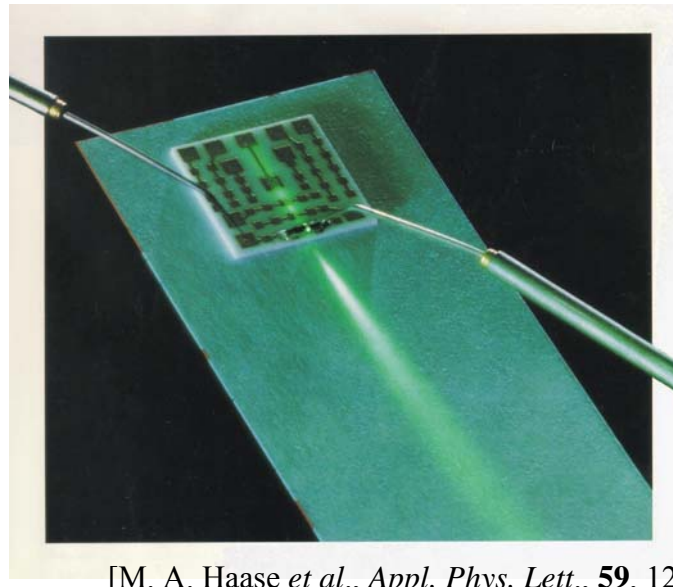
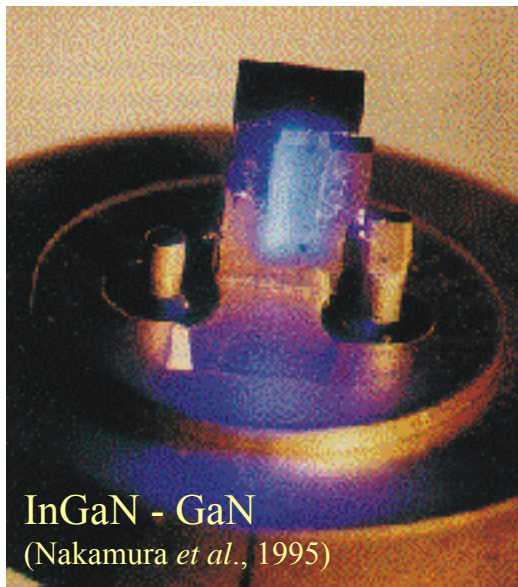


Strained heterostructures

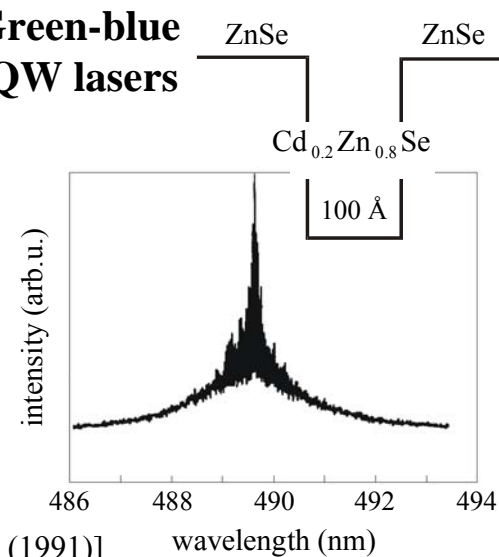


GaInAs – GaAs (Osborn *et al.*, ~ 1980)

GeSi – Si (Bean *et al.*, ~ 1980)



**Green-blue
QW lasers**



Resumé

NB

- math:

$$\int_a^b dx \delta(x - x_0) f(x) = f(x_0), \quad x_0 \in [a, b]$$

$$\delta(Cx) = \frac{1}{|C|} \delta(x)$$

Glossary:

- ultrathin QW's
- reflection / transmission amplitudes r , t and coefficients R , T – atspindžio ir pralaidumo amplitudės ir koeficientai
- band structure engineering – juostinės struktūros inžinerija
- strained heterostructures – įtempti heterodariniai

Further reading:

- V. Narayanamurti, *Phys. Today* **37**(10), 24 (1984)
- S. Nakamura, *Phys. World* **11**(2), 31 (1998)
- (Karpus 2004, p. 41–78)

Problems to solve:

- 2.9.4: 0.8pt, 0.6pt
- 2.9.5: [Kvantinė duobė ir stačiakampis barjeras 0.6pt](#), 0.6pt
- 2.9.6: 1pt, 0.2pt, 0.6pt